

Polaronic excitations in CMR manganite films

Ch. Hartinger, F. Mayr, and A. Loidl

EP V, Center for Electronic Correlations and Magnetism, University of Augsburg, 86135 Augsburg, Germany

T. Kopp

EP VI, Center for Electronic Correlations and Magnetism, University of Augsburg, 86135 Augsburg, Germany

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In the colossal magnetoresistance manganites polarons have been proposed as the charge carrier state which localizes across the metal-insulator transition. The character of the polarons is still under debate. We present an assessment of measurements which identify polarons in the metallic state of $\text{La}_{2/3}\text{Sr}_{1/3}\text{MnO}_3$ (LSMO) and $\text{La}_{2/3}\text{Ca}_{1/3}\text{MnO}_3$ (LCMO) thin films. We focus on optical spectroscopy in these films which displays a pronounced resonance in the mid-infrared. The temperature dependent resonance has been previously assigned to polaron excitations. These polaronic resonances are qualitatively distinct in LSMO and LCMO and we discuss large and small polaron scenarios which have been proposed so far. There is evidence for a large polaron excitation in LSMO and small polarons in LCMO. These scenarios are examined with respect to further experimental probes, specifically charge carrier mobility (Hall-effect measurements) and high-temperature dc-resistivity.

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I. INTRODUCTION

Since the discovery of the colossal magnetoresistance effect in thin films of $\text{La}_{2/3}\text{Ca}_{1/3}\text{MnO}_3$ by Helmolt *et al.*,¹ the properties of doped perovskite manganites have been a focal point of research in correlated electronic systems. These compounds reveal a variety of ordinary and exotic ground states, for example spin, orbital or charge order, cooperative Jahn-Teller (JT) distortions or electronic phase separation, as a result of a delicate interplay of orbital, spin, charge, and lattice degrees of freedom. While in the early days research concentrated on the appearance of colossal magnetoresistance (CMR), more recently also issues like orbital order, the importance of electron-phonon coupling, or phase separation scenarios promoted among the topics of interest. Optical spectroscopy, in both single crystals and thin films, has contributed to unravel the complex physics and provided insight into the importance of electron-phonon coupling for modelling the optical conductivity in the manganites.

Okimoto *et al.*² and Kaplan *et al.*³ reported on a large transfer of spectral weight from high to low energy with decreasing temperature for $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ single crystals and for $\text{Nd}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ thin films, respectively. The observed temperature dependence is consistent with the theoretical approach by Millis *et al.*,⁴ who went beyond Zener's double exchange⁵ and included dynamic JT polaron effects. Subsequent studies in crystalline^{6,7,8,9} and thin film^{10,11} samples confirmed the existence of the mid-infrared (MIR) excitation for a large number of manganites. In this context the concept of small (SP) and large polarons (LP) as essential ingredients to understand the electronic transport properties and the MIR excitation (labeled polaronic peak in the following) became subject of considerable theoretical efforts.^{4,12,13,14} In contrast to an optical transition between electronic bands, a characteristic feature of a polaronic absorption process is the significant frequency shift with temperature (see, for example, Ref. 15).

The shape of a polaronic resonance in the optical conduc-

tivity is predicted by theory whereby the details strongly depend on the nature of the polaronic excitations: large polarons exhibit a threshold behavior and a coupling dependent structure^{16,17} whereas small polarons display an asymmetric Gaussian peak;^{18,19} these latter polarons may even pair to form bipolarons with their own characteristics.^{14,20} The assignment "large" or "small" polaron usually refers to the spacial extension of the lattice distortion induced by a single charge carrier. True to the literature (for example, see the review by Emin on optical properties of polarons²¹) one would denote a lattice distortion generated by an electronic charge as a small polaron if it collapses to a single site — the smallest state compatible with the atomicity of a solid. Correspondingly, all polaronic states with extension larger than a lattice spacing are labelled large polarons. A large polaron does not necessarily extend over a large number of sites. However, since we have no direct means of determining the size of the polaronic cloud from optical spectroscopy, we instead refer to the related shape of the absorption spectra: threshold behavior for large polarons versus asymmetric Gaussian peak for small polarons.²¹

For the metallic manganites, a clear identification of the polaron type and the respective model is disputable not only because other electronic correlations may correct or even replace the standard polaronic physics but also because the statistics of the rather dense polaron system may strongly influence the shape of the resonance. Actually, small polarons which are trapped in a locally polarized lattice are less affected by finite doping. The MIR absorption may still be visualized in terms of transitions between the adiabatic levels of neighboring sites. The presence of other localized polarons at more distant sites will renormalize the polaronic energy scale (the binding energy) and it will raise the high-frequency wing of the resonance due to additional multi-polaron processes. However, a finite density should affect less the low-frequency wing, that is, absorption at energy less than the binding energy. In this work we will provide further optical conductivity and dc-resistivity data which confirm this small polaron sce-

nario for thin films of $\text{La}_{2/3}\text{Ca}_{1/3}\text{MnO}_3$ (LCMO).

By contrast, a large-polaron resonance should be influenced profoundly by a finite density of polarons due to their spacial extension and possible delocalization. A perturbational approach for small electron-phonon coupling at finite charge carrier density was presented recently by Tempere and Devreese (TD).²² In fact, if we compare the one-polaron absorption of Gurevich, Lang and Firsov (GLF)¹⁶ to the finite density result of TD, we notice that the low frequency behavior above the threshold is dictated by different power laws. Whereas the one-phonon absorption is characterized by a square root behavior, the fermionic statistics of many polarons leads to a linear density of states of particle-hole excitations at the Fermi edge which is in fact reflected in the threshold behavior of the absorption. In a recent paper²³ we proposed to identify the MIR resonance in thin films of $\text{La}_{2/3}\text{Sr}_{1/3}\text{MnO}_3$ (LSMO) by large polarons of this type.

Here we extend the preliminary discussion of our previous work in order to elucidate the distinct polaronic behavior in the metallic phase of manganites with strong (LCMO) and intermediate-to-weak electron-phonon coupling (LSMO). The purpose of our discussion is also, to a certain extent, a critical review of those polaronic models which have been proposed to identify the resonance in previous measurements with bulk samples. We observe that hitherto the proposed theoretical models are not capable of capturing all the aspects of a polaronic metal like LSMO. Notable details of the MIR spectra are in disagreement with the available theoretical models. A more comprehensive theory which offers an explanation particularly for the temperature-dependent shift of the polaronic resonance and for the magnitude of the spectral weight on the high-energy side would probably clarify the nature of the polaronic metal.

Using thin films in contrast to single crystals, we achieve a lower conductivity due to grain boundaries and strain.²⁴ Consequently screening is effectively reduced — to a level where phonons and polarons are well observable in the optical conductivity, even in the metallic phase. This allows the detailed analysis of phonons^{25,26} and polarons²³ from the respective optical data. Besides, the optical properties of single-crystal samples are more sensitive to surface preparation which, in particular, influences the MIR-region.²⁷

The role of the lattice mismatch on the structural and transport behavior in dependence of the film thickness has been systematically investigated in numerous articles. In particular it depends on the substrate/film combination and on the growth conditions. In general thicker films show a behavior very close to that of bulk²⁸ whereas substrate induced effects become more important in thinner films.²⁹

The structural differences between $\text{La}_{2/3}\text{Ca}_{1/3}\text{MnO}_3$, which is orthorhombically distorted, and $\text{La}_{2/3}\text{Sr}_{1/3}\text{MnO}_3$ with its rhombohedral symmetry represent promising conditions to distinguish between competing polaronic models. We discuss those models which adequately reproduce the low energy side of the resonance, as these excitations characterize the nature of the observed polarons.

II. EXPERIMENTAL ANALYSIS

A. Details and Characterization of the Films

The thin films were grown by a standard pulsed laser deposition technique³⁰ on plane-parallel $10 \times 10 \text{ mm}^2$ single crystalline substrates: LSMO on $(\text{LaAlO}_3)_{0.3}(\text{Sr}_2\text{AlTaO}_5)_{0.7}$ (LSAT) and LCMO on NdGaO_3 . Thin films with thickness between 200 nm and 400 nm were investigated. The nominale lattice mismatch is $<0.1\%$ for both.

X-ray diffraction (XRD) measurements were performed using a Bruker D8 Discover four circle x-ray diffractometer. In Fig. 1 we show x-ray diffraction patterns ($\Theta - 2\Theta$) obtained for LCMO on NdGaO_3 (upper panel) and LSMO on LSAT (lower panel). For LCMO/ NdGaO_3 the XRD displays only $(10l)$ diffraction peaks for Pnma and for LSMO/LSAT only $(l00)$ diffraction peaks for Pm3m symmetry. For both compounds there exist no indications of any impurity phase. This points to the highly oriented crystal growth of the films. The insets of Fig. 1 exhibit the rocking curves of the (202) peak for LCMO and the (200) peak for LSMO. Both films show a very narrow full width at half maximum (FWHM) of the rocking curve of 0.04° which give evidence for a high quality crystalline structure of the films.

Reflectivity measurements of the film-substrate system were carried out in the range of 50 to $4 \times 10^4 \text{ cm}^{-1}$ using the Fourier transform spectrometers Bruker IFS 113v and Bruker IFS 66v/S. Below room temperature the measurements were performed with a He-cryostat where the sample is placed in a static He exchange gas. The spectra at higher temperatures were taken in a home made oven in which the sample was exposed to a continuous flow of heated nitrogen gas. In addition, a Mach-Zehnder interferometer was used for ac measurements between 10 and 30 cm^{-1} which allowed to obtain both the intensity and the phase shift of the wave transmitted through the films on the substrate. Such transmission measurements of thin films have proven to be a powerful method for studying the electrodynamic properties of highly conductive thin films at low frequencies.³¹ The combined data sets improve the Kramers-Kronig (KK) analysis of the film-substrate system in the complete frequency range. For the analysis, the reflectivity $R(\omega)$ was extrapolated by a constant for frequencies below 10 cm^{-1} . For the high frequency region, the reflectivity between $4 \times 10^4 \text{ cm}^{-1}$ and 10^6 cm^{-1} was extrapolated by a $\omega^{-1.5}$ law. Above, a ω^{-4} dependence was assumed. The same procedure was utilized in separate experiments for the respective substrate. Applying the Fresnel optical coefficients for a two-layer system, the optical conductivity of the film was evaluated. A more detailed description of the data analysis is given in Ref. 32.

For room temperature the combined data sets of IR and ac reflectivity R are shown for the film-substrate system and for the bare substrate in the upper panel of Fig. 2 while the calculated conductivity σ is displayed in the lower panel. Most phonon resonances of the substrate are located in the minima of the film-substrate spectra. In the metallic phase the screening shields the lattice modes of the substrate, therefore only resonances of the thin film are visible. The temperature

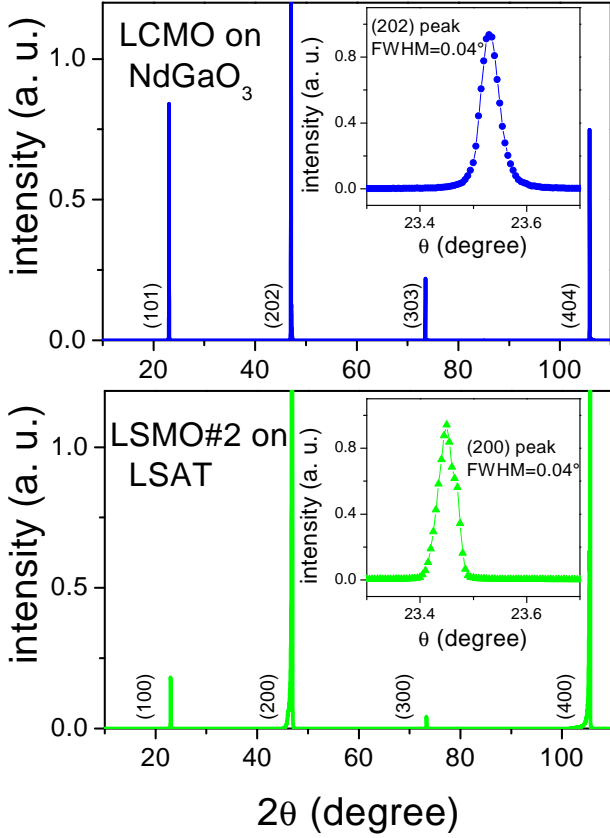


FIG. 1: (Color online) Room temperature $\Theta - 2\Theta$ XRD pattern for LCMO on NdGaO_3 (upper panel) and for LSMO on LSAT (lower panel). The insets show the rocking curve of the (202) peak and the (200) peak, respectively.

dependence of the phonon resonances provides for an exact determination of the film properties independently of the influence of the substrate. Moreover, the resonances known from neutron scattering measurements³³ are in good agreement with our results.

The electrical dc-resistivity of the films was measured with a standard four-point technique.²⁶ We estimate the defect level in relation to the single crystal. Due to stronger strain effects and a higher density of grain boundaries, the defect level in LSMO #2 is about 12 times higher and in LSMO #1 about 24 times than in the single crystal. For LCMO a single crystal was not available but the residual resistant is almost the same as for LSMO #2.

The magnetization was obtained with a commercial Quantum Design SQUID magnetometer. The measurements were carried out for the substrate and for the deposited film. The data were reported in a previous publication,²⁶ and a single crystal measurement is found in Ref. 25 for comparison. To characterize the ferromagnetic to paramagnetic (FM-PM) and the metal-insulator (MI) transition of the samples, we define T_C as the magnetic Curie temperature and T_{MI} is determined from the maximum of the dc resistivity curves. For LSMO the onset of spontaneous magnetization appears at 345 K, well be-

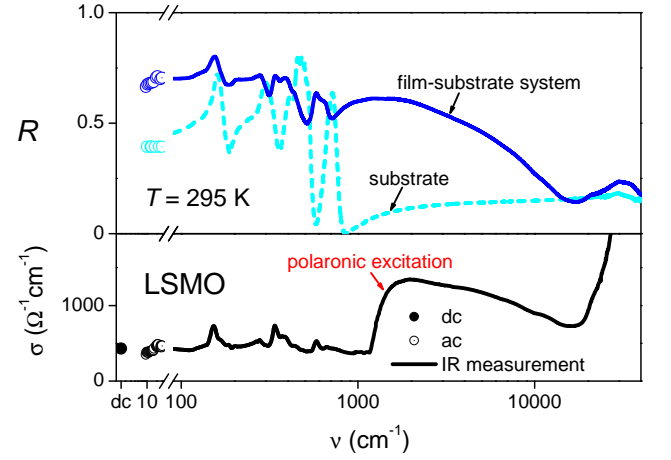


FIG. 2: (Color online) Upper panel: Reflectivity of the film-substrate system (LSMO on LSAT) and of the substrate itself (LSAT) at 295 K. Lower panel: The optical conductivity σ of the film, evaluated from the reflectivity data.

low $T_{MI} \approx 390$ K, while for LCMO $T_C \approx 243$ K coincides with T_{MI} .

B. Experimental Results

The reflectivity spectra for frequencies below the optical transitions are displayed in Fig. 3 for LSMO (upper panel)³⁴ and for LCMO (lower panel). The solid lines represent the spectra for temperatures in the metallic FM phase while the broken lines refer to those in the PM phase. The series of sharp peaks below $\sim 700 \text{ cm}^{-1}$ were identified as phonon modes. A detailed analysis of the phonon excitations in these films has been presented in a previous article.²⁶ The identification of the infrared-active phonons attests the quality of the thin films. In the following we focus on the excitation above $\sim 700 \text{ cm}^{-1}$, which has been assigned to polarons before.^{2,3,6,7,8,9,10,11,23}

For increasing temperatures the polaronic resonance in the optical conductivity continuously shifts to higher frequencies and, moreover, a loss of spectral weight is observed — as has been discussed in Ref. 23. Both quantities, frequency and amplitude of the resonance, will be listed in Tabs. I and II for LCMO and LSMO, respectively, linked to specific theoretical models. There is a remarkable difference in the shape of the polaron peak for LSMO and LCMO. In LSMO the shape is asymmetric and displays a steep slope below the peak position, whereas for LCMO the broader hump is more symmetric about its maximum and a low frequency threshold is entirely missing.

When we scale $\sigma(\nu)$ by a typical energy ν_0 of the polaronic resonance we find a universal low-energy slope for the LSMO spectra (upper panel of Fig. 4) whereas this scaling behavior is absent in the LCMO spectra (Fig. 4, lower panel). For this presentation, ν_0 is the threshold on the low-energy side of the MIR-resonance of the LSMO spectra and the frequency at the

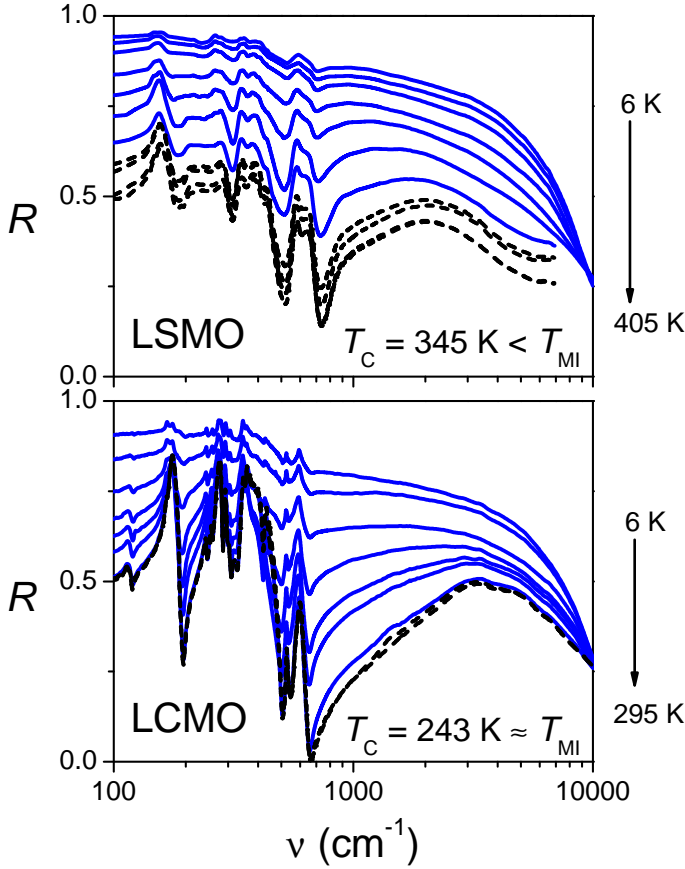


FIG. 3: (Color online) Reflectivity spectra for LSMO on LSAT (upper panel) and LCMO on NdGaO₃ (lower panel) over a temperature range from the metallic to the insulating phase. The solid lines represent spectra in the FM phase, the broken lines in the PM phase.

maximum of the MIR resonance of the LCMO spectra, respectively. To retrieve the threshold frequency ν_0 for LSMO, one has to take into account that a background adds to the polaronic absorption close to the threshold. We assume that the 295 K data approximately display the background for the considered frequency window: the phonon resonances are sufficiently far below ν_0 so that they should interfere very little with the polaronic resonance, and the frequency dependence of the intensity of excitations responsible for the background is negligible for the considered frequency window in which we address the scaling behavior. We then extrapolate the low frequency slope of the curves at all other temperatures to this “zero line” in order to identify ν_0 . Strictly speaking, ν_0 depends slightly on the extrapolation procedure. This qualitative distinction of the LSMO and LCMO spectra has to be addressed in a thorough theoretical modelling.

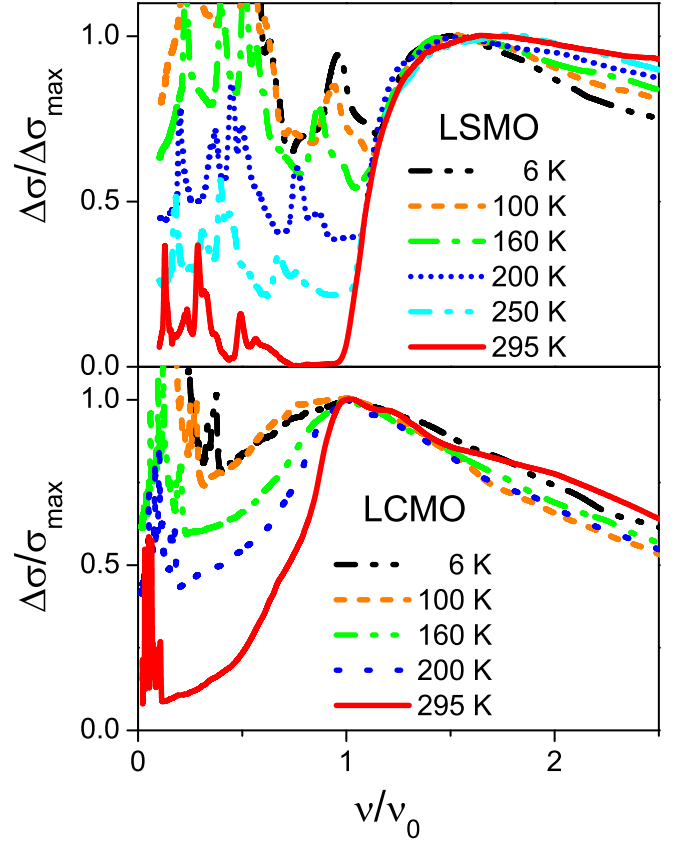


FIG. 4: (Color online) Rescaled optical conductivity of LSMO (upper panel) and LCMO (lower panel): the optical conductivity is scaled by the maximum of the MIR resonance. A constant background of $\sigma_{\text{bg}} = 370 \, \Omega^{-1} \text{cm}^{-1}$ for $\Delta\sigma$ is subtracted for LSMO (for details, see main text). The frequency is scaled by the threshold value ν_0 of the onset of the polaronic peak for LSMO, while for LCMO by the peak maximum. Clearly, the scaling behavior of the low frequency slope is missing for the LCMO spectra.

III. FURTHER EVIDENCE FOR SMALL AND LARGE POLARON SCENARIOS

A. Holstein SP hopping

The MIR optical conductivity displays distinct polaronic excitations for LSMO and LCMO. It is expected that this distinction also manifests itself in a disparate dc-resistivity for the two types of manganite films.

In Fig. 5 we show the high temperature dc-resistivity of LSMO (upper panel) and LCMO (lower panel) in a $\ln(\rho/T)$ vs. $1/T$ scale. In the lower plot a linear dependence for the latter compound above T_{MI} is clearly visible. Slightly above T_{MI} , which coincides with the magnetic ordering temperature, deviations from the thermally activated behavior occur. It is widely accepted that the electron-phonon coupling is sufficiently large to localize the carriers in the paramagnetic phase — presumably in combination with other localization mechanisms. Over a temperature range from 255 – 560 K

the electrical dc-resistivity is well described by the adiabatic SP model³⁵ (lower panel) with a dc activation energy $E_a = 672 \text{ cm}^{-1}$, which is in agreement with previously reported results.^{20,24,36,37} In general the binding energy E_b of the SP in the optical data (see Tab. I) is related to the activation energy of the transport data by $E_b = 2E_a$. The maximum in the optical conductivity in the paramagnetic phase ($T = 250 \text{ K}$) is located around 6040 cm^{-1} , which is rather $8E_a$ than the theoretically expected $2E_b = 4E_a$. The discrepancy between the transport value and the optical value is not surprising since it was also observed in other polaronic systems³⁸ (including the classical small polaron material TiO_2 ; the difference has been discussed by Reik³⁹ and Austin,⁴⁰ and for the manganites by Hohenadler and Edwards⁴¹).

Neutron scattering measurements for single crystal sample were interpreted in terms of "single polarons" and "correlated polarons" (see, e.g. Ref. 42,43) — the existence of which is supposed to be consistent with a phase separation scenario.⁴⁴ Alvarez *et al.*⁴⁵ predict uncorrelated magnetic clusters in a temperature range $T_C \leq T \leq T^*$. Below T_C the clusters align their moments. Above T^* single polarons are expected to dominate the transport.⁴⁴ In fact, for LCMO we find a kink in the high temperature dc-resistivity data (see $\ln \rho(T)$ in the inset of Fig. 5). We tentatively identify this kink at 560 K with T^* . This observation is qualitatively consistent with film and single crystal results reported in Ref. 24 but we question their interpretation according to which the kink is a signature of a structural transition. Rather it appears that the different slopes depend on various scattering processes of correlated and single polarons, and the temperature T^* characterizes the crossover.

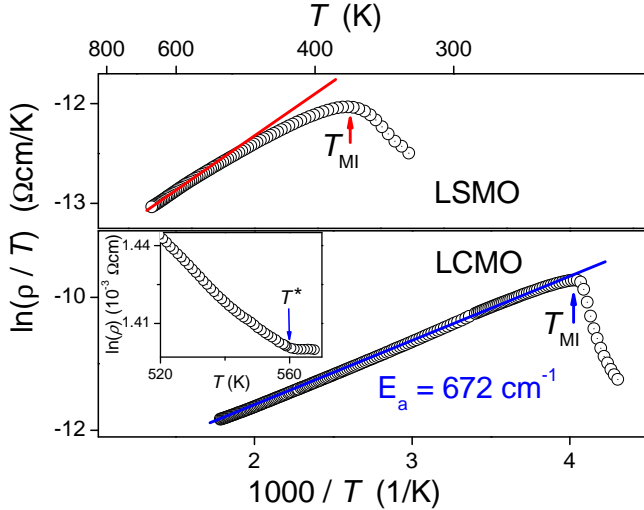


FIG. 5: (Color online) High temperature dc-resistivity of LSMO (upper panel) and LCMO (lower panel). The solid lines are the fit of the adiabatic SP model. For LCMO the curve is linear and corresponds to polaron conduction with an activation energy $E_a = 672 \text{ cm}^{-1}$. The inset displays a kink in the dc-resistivity of LCMO at 560 K which we identify with T^* (see main text).

Previously, it has been reported that correlated polarons have been found only in the orthorhombic phase (LCMO).⁴⁶ This observation may be related to the distinct high temperature behavior in LCMO and LSMO. For LSMO we identified LP-type excitations from the optical conductivity data. Figure 5 (upper panel) shows the high temperature dc-resistivity from 330 – 750 K. Clearly, the adiabatic SP model (solid line) provides a poor fit to the experimental data (compare the discussion in Ref. 47).

The temperature dependence of the JT distortion for $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ has been investigated more recently by Manella *et al.*^{48,49} with x-ray absorption spectroscopy. They provide direct experimental evidence for the presence of polarons in the paramagnetic state and analyze the dopant dependence of the JT distortion. Specifically, the variance of the Mn-O bond length distribution in the Sr doped sample was shown to be only half that in the Ca doped sample.

B. Charge Carrier Mobility

Further support for the SP concept in LCMO and the LP ansatz in LSMO comes from the literature on the polaron mobility. Figure 6 compares the temperature dependence of the dc- and ac-conductivities (right axis) with the mobility (left axis) obtained by Hall-effect measurements by Jakob *et al.*⁵⁰ The carrier mobility decreases with increasing temperature in the FM phase. Above T_{MI} the mobility increases slightly. All three measurements show the same overall temperature behavior. The deviation close to T_{MI} may be due to different coupling mechanisms of the local transport properties to critical magnetic fluctuations.

The decrease of the mobility in the FM phase corresponds to the increase of the effective electron-phonon coupling (polaron energy over bandwidth). Moreover, the spectral weight of the polaronic excitation is reduced on increasing

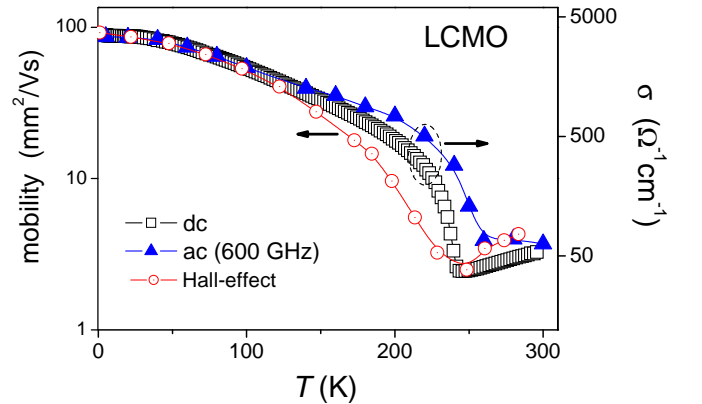


FIG. 6: (Color online) For LCMO the temperature behavior of dc and ac electrical conductivity σ (right axis) corresponds to the temperature dependence of the mobility (left axis) obtained from Hall-effect measurements.⁵⁰ The similarity of the data indicates a common physical origin.

temperature.²³ As a consequence, with decreasing lattice distortions, the tendency to charge localization is reduced.

For LSMO only few Hall effect studies have been reported, none of them providing values of the polaron mobility μ_H .^{47,51,52} Therefore, only a rough estimate as $R_H/\rho_{xx} \approx 400 \text{ mm}^2/\text{Vs}$ at 4.2 K is possible,⁵² which is four times larger than in LCMO (Fig. 6). The ratio of the mobilities corresponds well to the ratio of the effective masses of specific-heat measurements,⁵³ and reveals the expected tendency. We propose that optical and Hall transport consistently support the applicability of a LP-type approach. This interpretation is also in agreement with neutron scattering results where the spatial extension of the polaron covers several lattice constants at low temperatures: Louca and Egami⁵⁴ investigated deviations of the local structure from the average crystal structure in $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ by pulsed neutron scattering with pair distribution function analysis. X-ray absorption fine structure measurements^{48,55} differ for the metallic phase quantitatively, but all groups identify a temperature-dependent lattice distortion.

IV. DISCUSSION OF THE MIR SPECTRA

Early on the double exchange (DE),^{5,56} in combination with a strong Hund coupling, was identified as a key element to explain the interrelation between metallicity and ferromagnetism in the doped manganites. It has only recently been understood that further basic mechanisms have to be an integral part of a comprehensive model that can explain magnetotransport properties and the transition to the paramagnetic phase. Millis, Littlewood and Shraiman⁵⁷ elaborated that the DE mechanism is not sufficient to reproduce the measured resistivity for temperatures of the order of T_C . They suggested that, in the presence of a strong electron-phonon coupling, polaronic effects have to be included. Dagotto, Hotta and Moreo⁵⁸ promoted that intrinsic inhomogeneities are generated through the cooperative effect of phase separation tendencies, long-range Coulomb interaction and disorder, and these inhomogeneities are supposed to dominate the transport behavior.

In the following discussion on the nature of the MIR resonance, we will consider only the polaronic models with no refinement of electron-electron interactions or disorder physics. This disregard of some of the essential ingredients of a comprehensive microscopic model for manganites is in general not justified. However, a solution to such a “comprehensive model” is at present not available, certainly not for an authoritative evaluation of the MIR optical conductivity. On the other hand, some of the electronic correlations missing in the polaron models would enter only as effective parameters, such as the temperature-dependent kinetic energy, or the projection on one spin direction. Consequently, these correlations do not necessarily have to be disentangled from a more microscopic modelling. Finally, the purpose of our discussion is also a critical review of the polaronic models which have been previously related to the resonance. We reemphasize that in the considered thin films, the resonance is more pronounced and

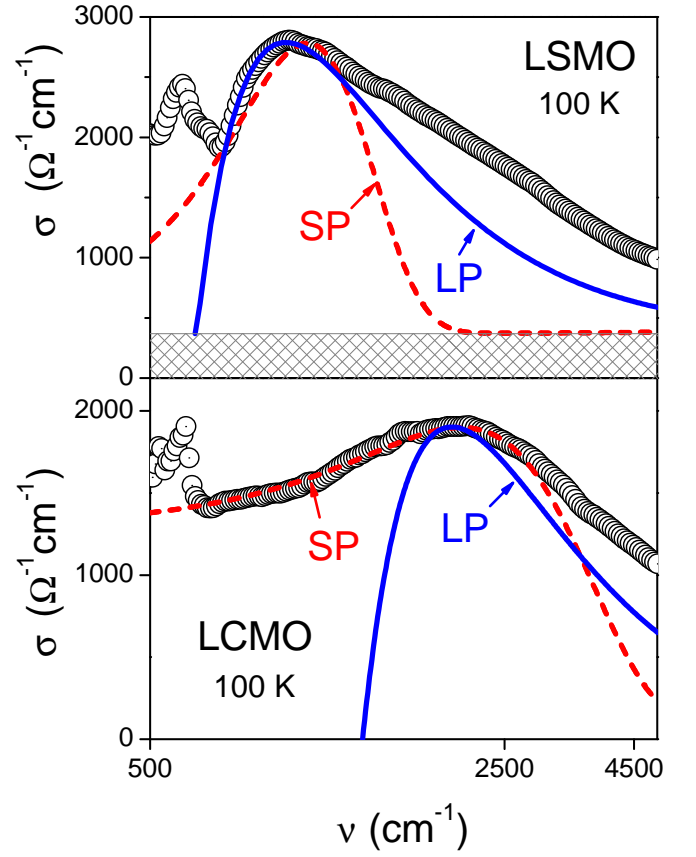


FIG. 7: (Color online) The optical conductivity spectra of LSMO (upper panel) and LCMO (lower panel) at 100 K (data points) on a logarithmic frequency scale. For a preliminary assignment to large polarons (LP, solid line) and small polarons (SP, dashed line), Eqs. (8) and (1) have been used for the respective fits.

the shape is well resolved so that a refined analysis is now attainable with our data.

A small polaron in the regime of sufficiently strong electron-lattice coupling is excited from a site-localized state to another well-localized state at an adjacent site.⁵⁹ The maximum of the absorption, that is the most probable process, is the Franck-Condon like transition with frequency ω_m four times the activation energy for the intersite transition.^{39,60} The MIR conductivity then has the form of an asymmetric Gaussian peak centered around ω_m . Whereas the optical conductivity of LCMO approaches this shape and therefore is identified as a small polaron, the optical conductivity of LSMO does not (compare Fig. 7).

A large polaron is observed usually in the weak coupling regime. Then, to first order in the electron-lattice coupling, the optical absorption is the excitation of a phonon with a simultaneous excitation of the charge carrier GLF¹⁶. Consequently, one finds a threshold behavior at the (optical) phonon frequency with a sharp increase in the absorption rate due to the available scattering states and a slow decrease at the high-energy side controlled by a $1/\omega^3$ -factor, most easily identified in the force-force correlation function form of the

conductivity.⁶⁰ For intermediate to strong electron-lattice coupling, if the polaron is in a self-trapped state, the threshold is determined by the polaron binding energy, with the charge carrier scattering into an extended state (Emin²¹ assumes a free-carrier state). The initial upturn of the absorption spectrum is again given by the phase space of the available scattering states. The shape of the observed optical conductivity appears to be qualitatively similar to that in the GLF- and Emin-approaches, and we tentatively identify the polaronic resonance for LSMO as the excitation of a large polaron (see Fig. 7). The validity of such models to the manganite films will be investigated in the following sections.

The asymmetric shape of the MIR resonance with the steep increase on the low-energy side is quite spectacular for the investigated LSMO films. As argued before, the upturn of the optical conductivity above the threshold is controlled by phase space considerations. For example, if the electronic states created by the absorption process are particle-hole excitations close to a Fermi edge, the number of such states increases linearly with the energetic distance (frequency) to the edge. Whatever the details, one may expect a scaling behavior of LSMO, at least for the initial increase above the threshold. This scaling would signify that the low energy scattering processes are of the same origin, independent of temperature, related band narrowing and other energy scales. In fact, a universal low-frequency slope has been verified for the LSMO spectra (Fig. 4, upper panel) but it is absent for LCMO which neither displays a threshold on the low-energy side of the MIR-resonance (Fig. 4, lower panel).

A. Small polarons in LCMO

Various experimental data sets on both, ferromagnetic and paramagnetic manganites, have been interpreted in terms of the Holstein small-polaron theory³⁵ (see our previous section, and also the critical discussion on this issue in Ref. 61). An extension of the standard SP optical conductivity formula^{19,39} has been proposed for the evaluation of the low-temperature optical spectroscopy:^{62,63}

$$\sigma(\omega, T) = \sigma(0, T) \frac{\sinh(4E_b \hbar\omega / \Delta^2)}{4E_b \hbar\omega / \Delta^2} e^{-(\hbar\omega)^2 / \Delta^2} \quad (1)$$

$$\Delta \equiv 2\sqrt{2E_b E_{\text{vib}}}$$

Here E_b is the SP binding energy, $\sigma(0, T)$ is the dc conductivity, Δ signifies a broadening, and E_{vib} is the characteristic vibrational energy, which is $E_{\text{vib}} = k_B T$ in the high-temperature regime and $E_{\text{vib}} = \hbar\omega_{\text{ph}}/2$ at low temperatures ($k_B T < \hbar\omega_{\text{ph}}$). Eq. (1) constitutes a broad resonance with a maximum at $\hbar\omega_m \approx 2E_b$. For high temperatures, the dc-conductivity results from the thermal activation over the potential barrier ($E_b/2$) between adjacent sites and the optical conductivity peaks at the frequency ($2E_b$) of the Franck-Condon-like transition for neighboring potential energy curves, which are approximately parabolic in the configurational coordinates. For low temperatures, the processes

are similar, however the phonons which participate in the activated hopping are not thermal.

The dashed lines in Fig. 7 present the optical conductivity of a SP, Eq. (1). The shape for low frequencies, including the maximum, is well reproduced for LCMO. The SP model nicely describes the experimental results for 100 K using $2E_b = 2820 \text{ cm}^{-1}$ and a characteristic phonon energy $E_{\text{vib}} = 270 \text{ cm}^{-1}$. The disagreement between theory and experiment for higher frequencies is not unexpected (it has also been observed for the classical small polaron material TiO_2 , and several mechanisms were proposed to account for the difference;⁶⁴ see also the SP evaluation for the $2d$ nickelates and cuprates³⁸). As seen from Tab. I and Tab. III, with rising temperature the polaron formation energy increases. For LCMO the binding energy ($2E_b$) rises from 2210 cm^{-1} (6 K) to 6040 cm^{-1} (250 K). Above the metal-to-insulator transition at T_{MI} , the polaron formation energy remains constant.

Whereas one may expect that the *low-energy* SP absorption is well explained by the processes described above — since they are local —, one has to consider the consequences of a high polaron concentration and Fermi energy for the *high-energy* SP absorption in order to understand the slow decay observed in experiments. Especially for temperatures of the order of T_C polaron-polaron interaction appears to be strong,^{42,43} however a relation to the high-energy slope of the polaronic MIR resonance is not evident.

An explanation of the high energy decay and of the temperature dependence of the polaron binding energy is beyond the scope of this paper. A transfer of spectral weight towards higher energies was discussed within a dynamical mean field theory of the Holstein model by Fratini *et al.*,⁶⁵ however, their treatment only applies to a dilute nondegenerate polaron gas. The shape and position of the polaronic MIR resonance for a model with Fermi edge and a finite concentration of polarons has been investigated by Millis, Mueller and Shraiman (MMS).⁴ They study the DE model with a JT form for the electron-phonon coupling. The local phonons are taken as classical harmonic oscillators, and the electronic correlations are evaluated within the DMFT scheme. For half filling ($n_{e_g} = 1$, with the e_g orbitals singly occupied) and intermediate coupling, MMS compare their optical conductivity favorably with the data of Okimoto *et al.*^{2,66} for $\text{La}_{0.875}\text{Sr}_{0.125}\text{MnO}_3$ — and for somewhat stronger coupling with the data of Kaplan *et al.*³ for $\text{Nd}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$. Also our optical data agree qualitatively with the latter results of MMS though the high frequency side again decays too fast in the model evaluation. The broad peak is due to transitions between the two JT split levels with a strongly fluctuating phonon coordinate. The ac-

TABLE I: Fit parameters of the optical conductivity for LCMO at different temperature using the SP formula, Eq. 1.

T (K)	6	100	160	200	220	240	250
σ_0 ($\Omega^{-1}\text{cm}^{-1}$)	1410	1270	930	685	410	130	90
$2E_b$ (cm^{-1})	2210	2820	3720	4080	5020	5700	6040
E_{vib} (cm^{-1})	217	270	340	335	330	270	270

tual results for the evaluation of doped systems are less favorable: a second peak below is formed which is due to transitions to unoccupied sites with no JT splitting. It appears to contradict the observations. However, MMS argue that further electronic correlations which have not been included can remedy this shortcoming.

Some of the quantum fluctuations missing in MMS are included in the “many-body CPA” treatment of the Holstein-DE model⁶⁷ for which Hohenadler and Edwards⁴¹ compare the MIR optical conductivity with the measurements³ for $\text{Nd}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$. The shift of spectral weight to lower frequencies with decreasing temperature is still insufficient. Peroni *et al.*⁶⁸ propose that their variational Lang-Firsov treatment recovers the low temperature behavior,^{69,70} including a Drude peak.

B. Bipolaron theory for the optical conductivity

The crossover from the paramagnetic to the ferromagnetic phase in the optical absorption has been studied by Alexandrov and Bratkovsky¹⁴ in terms of a bipolaron model in which the optical intraband conductivity should be provided by two different polaronic contributions originating from SP and bipolarons with different binding energies. Accordingly, in the PM phase the optical conductivity would be dominated by small bipolaronic charge carriers, which break up at the magnetic transition, leaving only SP which then dominate the MIR excitations in the FM regime. As a result, a sudden transfer of spectral weight at T_C is predicted along with a sharp drop in the dc-resistivity due to the charge carrier collapse. As such a transfer is not confirmed by our data, we rather discard such a scenario for LSMO and LCMO, even though the oxygen-isotope effect on the thermoelectrical power in several ferromagnetic manganites seems to provide experimental clues for bipolaron formation.²⁰

C. Large polarons in LSMO

We will now inquire if models, which have been recently proposed in this context, indeed reproduce the observed scaling and threshold behavior for LSMO. For this purpose, we organize this Section IV C as follows:

In a first approach we will use a well-controlled weak coupling scheme (see Sec. IV C 1) which follows from a RPA-evaluation of the Hubbard model to which a Fröhlich type electron-phonon coupling has been added. As we only consider the ferromagnetic metallic state we restrict the evaluation to the spin polarized sector (spinless fermions). The local interaction U signifies the on-site interaction between charge carriers in the two e_g -orbitals. The RPA-results well approximate the low-frequency slope of the polaronic resonance and reproduce the observed scaling. In fact, the model replicates the most prominent and important characteristics of the polaronic spectra in LSMO. However it fails to treat the high energy features adequately.

In a second approach we investigate intermediate and strong coupling schemes for large polarons (see the end of Sec. IV C 1 and the Section IV C 2 on *self-trapped polarons*). The latter scheme was proposed recently,⁷ in order to identify the MIR absorption processes in bulk manganites as excitations from a localized self-trapped state to free-carrier continuum states (the authors of Ref. 7 refer to the model presented by Emin in Ref. 21). The shape of the polaronic resonance in LSMO is well reproduced for the low energy side and the model may account for a shift of the threshold energy with increased binding (at higher temperatures). However the theoretical (strong coupling) estimate of the polaron radius differs significantly from the radius which fits the experimental data. Moreover, the approach does not apply when a Fermi surface of the (free) charge carriers is formed.

Finally, in Sec. IV C 3 we discuss the consequences when charge carriers are excited from a potential well to a Fermi surface. The collective behavior associated with the response of the Fermi sea to the transition determines the shape of the resonance in the adiabatic limit (in which the potential well decays slowly with respect to the fast electronic transition). A full evaluation of this fascinating scenario is not yet available.

1. Weak coupling scenario

The shape of the MIR resonance in the LSMO films is reminiscent of the weak coupling result by GLF for Fröhlich polarons (see, for example, Ref. 60 and Eq. (4) below). A closer inspection reveals that the width of the GLF absorption is too small and the low-frequency slope is too steep to fit the LSMO data (see Fig. 8). This failure is not unexpected since we have 10^{21} – 10^{22} charge carriers per cm^3 , as identified from Hall measurements.⁵¹ An extension of the GLF weak-coupling polaron theory to a finite concentration has been carried out by Tempere and Devreese.²² In their work on *optical absorption of an interacting many-polaron gas*, they found a remarkable agreement between their theoretical prediction and the experimental curve for $\text{Nd}_2\text{CuO}_{4-y}$ ⁷¹ in the optical conductivity around 1000 cm^{-1} . We now transfer their approach to the manganites.

The real part of the optical conductivity $\sigma(\omega)$ is expressed through a momentum integral over the dynamical structure factor $S(q, \omega)$ which is in three space dimensions:^{22,60}

$$\sigma(\omega) = \alpha n_p \frac{2}{3} \frac{e^2}{m^2} \frac{(\hbar\omega_0)^2}{\pi\hbar\omega^3} \sqrt{\frac{\hbar}{2m\omega_0}} \int_0^\infty dq q^2 S(q, \omega - \omega_0) \quad (2)$$

Here, n_p is the polaron density, m is the effective mass of the charge carriers, α is the electron-lattice coupling and $\hbar\omega_0 = \hbar\nu_0$ is the threshold energy for polaronic absorption (in weak coupling, it is the energy of the respective optical phonon). The dynamical structure factor is expressed in terms of the dielectric constant $\epsilon(q, \omega)$:⁶⁰

$$S(q, \omega) = \frac{\hbar}{n} \frac{q^2}{4\pi e^2} \Im \left[-\frac{1}{\epsilon(q, \omega)} \right], \quad (3)$$

where n is the density of charge carriers which should be identified with the polaron density n_p for the considered finite concentration. TD evaluated Eq. (2) to linear order in α which implies that $S(q, \omega)$ is taken to zeroth order in the electron-lattice coupling. The dielectric constant is then approximated by the Lindhard (or RPA) expression for the homogeneous electron gas. In this linear approximation (with respect to α), TD argue that, for the low-density limit, the GLF result is recovered. Indeed, for fermions with one flavor, the structure factor approaches⁷² $S(q, \omega)_{k_f \rightarrow 0} \rightarrow 2\pi\delta(\omega - \varepsilon_q/\hbar)$. The optical conductivity assumes the limiting form of GLF¹⁶ (cf. Fig 8):

$$\sigma(\omega)_{k_f \rightarrow 0} \rightarrow \alpha n_p \frac{2}{3} \frac{e^2}{m} \frac{1}{\omega_0} \left(\frac{\omega_0}{\omega}\right)^3 \sqrt{\frac{\omega}{\omega_0} - 1} \quad (4)$$

For the manganites in the investigated ferromagnetic, metallic regime with a carrier density of 10^{21} – 10^{22} cm^{-3} , we take the following standard simplifications for the low-temperature evaluation: (i) only one spin direction prevails (spinless fermions), due to DE and strong Hund coupling, (ii) there are two degenerate orbital states (the two e_g -levels); accordingly we deal with two flavors for the fermionic particles, (iii) the interaction is represented by the local Hubbard U for two fermions on the same site in two e_g orbital states, and not by the long-range Coulomb interaction $v_q = 4\pi e^2/q^2$, (iv) the fermions acquire a quadratic dispersion. The last assumption may be refined to the appropriate two-band dispersion of the e_g -levels. However, for the discussion of the optical conductivity it is of minor importance, especially when we primarily discuss the low-frequency excitations with energy much less than the Fermi energy. Furthermore, a dynamical JT effect is not implemented: it is entirely missing in this weak coupling approach of TD.

The longitudinal dielectric response in the Hubbard model (with quadratic dispersion) is in RPA:

$$\epsilon(q, \omega) = 1 - \frac{3}{4} \frac{U}{E_f} \left\{ 1 - \frac{1}{(2x)^3} \left[((x^2 - y)^2 - 4x^2) \ln \frac{x^2 - y + 2x}{x^2 - y - 2x} + ((x^2 + y)^2 - 4x^2) \ln \frac{x^2 + y + 2x}{x^2 + y - 2x} \right] \right\} \quad (5)$$

$x \rightarrow q/k_f$
 $y \rightarrow \hbar\omega/E_f + i0$

The related expression for the Coulomb gas⁷³ is usually not presented in a closed form. Here care has been taken to ensure that this closed expression for the dielectric response is valid for all complex values of y .

The optical conductivity is (cf. the similar expression in Ref. 22 for the Coulomb gas model)

$$\sigma(\omega) = \alpha \gamma \delta \int_0^\infty dx x^2 \frac{4}{3} \frac{E_f}{U} \left(\frac{\omega_0}{\omega}\right)^3 \Im \left[-\frac{1}{\epsilon(x, \omega - \omega_0)} \right], \quad (6)$$

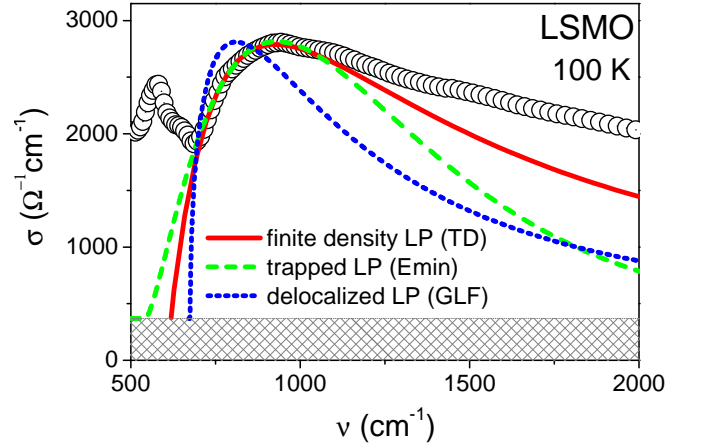


FIG. 8: (Color online) Comparison of the low temperature (100 K) optical conductivity (in the MIR range of the polaronic excitations) to the results from various model calculations: the continuous line refers to the weak coupling approach of Tempere and Devreese modified for an on-site Hubbard interaction, Eq. (6); the dashed line is the result of the phenomenological approach for self-trapped large polarons by Emin, modified to Gaussian localized states, Eq. (9); the dotted curve is the weak coupling single-polaron result by Gurevich, Lang and Firsov, Eq. (4). The appropriate parameters for each of these model evaluations are given in the main text.

whereby

$$\gamma = n_p \frac{2}{3} \frac{e^2}{m} \frac{1}{\omega_0}$$

is the prefactor which already appears in the GLF-limit, and

$$\delta = \frac{3}{2\pi} k_f \sqrt{\frac{\hbar}{2m\omega_0}}$$

is a dimensionless prefactor which accounts for the finite charge carrier density. The integration variable x in Eq. (6) is the normalized wavevector $x = q/k_f$. The dielectric response in the Hubbard model, Eq. (5), and the optical conductivity, Eq. (6), are in a simple way related to the respective expressions for the Coulomb gas if we substitute in Eqs. (5) and (6) the interaction parameter by

$$\frac{3}{4} \frac{U}{E_f} \longrightarrow \frac{\xi}{x^2}, \quad (7)$$

where ξ is the dimensionless interaction strength of the Coulomb gas, $\xi = e^2 k_f / (\pi E_f)$.

Finally, we adjust the parameters tentatively in the following way: a) the density of charge carriers is $6 \times 10^{21} \text{ cm}^{-3}$, which is the stoichiometric number of doped holes and which is in the range of what has been estimated from Hall measurements,⁵¹ b) we take m three times the bare electronic mass ($m = 3m_e$) which is consistent with specific heat measurements,⁷⁴ c) since $E_f = 3270 \text{ cm}^{-1}$ for the density of (a) and for the effective mass of (b), and since we read from the 100 K data $\nu_0 = 617 \text{ cm}^{-1}$ we fix $\hbar\omega_0/E_f = 0.19$, that

is, we are in the adiabatic regime, and d) $U/E_f = 0.2$ in order to start, for a first estimate, with small electronic interactions for which RPA is a reasonable approach.

For this parameter set we find from Eq. (6) a shape of the polaronic resonance (see Fig. 8) which reproduces well the experimental data for frequencies up to the maximum. The high energy slope, however, decreases more rapidly than in the measured optical conductivity. The maximal optical conductivity is, in our calculation, $\sigma_{\max} = \alpha \times 1.84 \times 10^3 \Omega^{-1}\text{cm}^{-1}$ which should fit the data with $\alpha \simeq 1.3$ — whereby the shaded background in Fig. 8 is to be subtracted.

If we had taken the Coulomb gas (as TD did for $\text{Nd}_2\text{CuO}_{4-y}$) with the same density, effective mass and the same ratio $\hbar\omega_0/E_f$ as above for the Hubbard model, we would find nearly the same line shape (not distinguishable in the plot). The dimensionless interaction strength then is $\xi = 6.5$ and the plasma frequency is at $\hbar\omega_{\text{plasma}}/E_f = 4.15$. Since the plasmon is consequently far outside the frequency window of our investigation it is not surprising to have similar results for the Coulomb-gas and Hubbard-model approach for these reasonably large densities. However, the maximal optical conductivity is $\sigma_{\max} = \alpha \times 0.11 \times 10^3 \Omega^{-1}\text{cm}^{-1}$ in the Coulomb gas case. This implies an electron-lattice coupling α of the order of 20, which is probably too large⁷⁵ by a factor of 5 to 6 — apart from the fact that the Coulomb gas model is not quite appropriate for these manganites. We conclude that the Hubbard model, rather than the Coulomb gas approach, is the proper model Hamiltonian provided that also an electron-phonon coupling term is added.

The solution, Eq. (6), suggests to determine the model parameters through an “optimal fit”, now including the high frequency slope. The shape of the optical conductivity in this approach only depends on $\hbar\omega_0/E_f$, and the fine tuning fixes the value of U/E_f . For small values of $\hbar\omega_0/E_f$, such as for the above value 0.19, the absorption shape is nearly independent of U/E_f , except that the magnitude (σ_{\max}) scales down with increasing U/E_f .⁷⁶ A better fit is found with larger values of $\hbar\omega_0/E_f$. The optimal values are $\hbar\omega_0/E_f = 0.9$ and $U/E_f \simeq 4$ (see Fig. 9). If we again assume that the density of charge carriers is $6 \times 10^{21} \text{ cm}^{-3}$, we are constrained to $m/m_e = 14.3$. Alternatively, we could fix $m/m_e = 3$ but then we have to assume a strongly reduced polaron density of $0.6 \times 10^{21} \text{ cm}^{-3}$. The drawback of this “optimal fit” however is that $\sigma_{\max}/\alpha = 0.05 \times 10^3 \Omega^{-1}\text{cm}^{-1}$, in the first case, and $0.02 \times 10^3 \Omega^{-1}\text{cm}^{-1}$, in the second case, both of them too small to be reasonably close to experiment. We deduce from this investigation that the high energy side cannot be satisfactorily captured within this model. The high energy slope with its complex cooperative excitations has to be explored with more involved theoretical concepts which necessarily depend on a larger parameter set. However, this does not invalidate the evaluation for the universal low energy side.

For the 6 K data, the low energy side of the polaronic resonance was fitted successfully in our previous paper.^{23,34} For the sample presented here we find $\nu_0 = 593 \text{ cm}^{-1}$, which implies that $\hbar\omega_0/E_f = 0.18$. With $U/E_f \simeq 0.2$ we have a nearly identical fit to that of Fig. 4 in Ref. 23 which generates sufficient spectral weight so that the electron-phonon

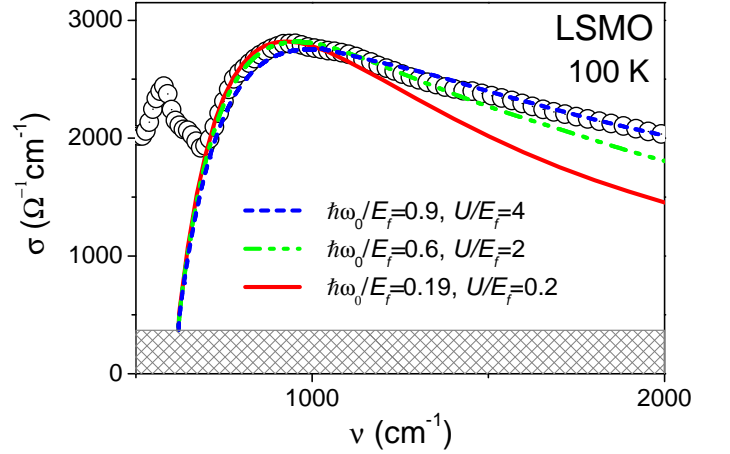


FIG. 9: (Color online) In the RPA-approach, Eq. (6), the shape of the optical conductivity depends on the model parameters $\hbar\omega_0/E_f$ and U/E_f . For the adiabatic weak-coupling case ($U/E_f = 0.2$, $\hbar\omega_0/E_f = 0.19$) the approximate form, Eq. (8), is indistinguishable from the full RPA-result, Eq. (6). For details of the comparison between the experimental 100 K data and the theoretical results see the main text.

coupling α can be chosen to be of order 1. This situation is qualitatively similar to that with the 100 K data. The same applies to higher temperatures. We may assume that temperatures as high as 295 K are still considerably smaller than the Fermi energy. Then temperature does not explicitly enter the dynamical response but it is supposed to tune the band width, and correspondingly the Fermi energy and effective mass, and possibly ω_0 (see the discussion below on this last presumption).

Assessment of the weak coupling approach. From the above discussion we deduce that a value of $\hbar\omega_0/E_f \simeq 0.2$ and $U/E_f < 0.5$, is a reasonable choice for low temperatures to acquire sufficient optical weight in this approach. Thereby, the precise values of U/E_f and $\hbar\omega_0/E_f$ just control the overall magnitude of the polaronic resonance provided that $\hbar\omega_0/E_f \ll 1$ applies.⁷⁷ Furthermore, for the considered frequency range above the threshold, we are always sufficiently close to the Fermi edge in order to approximate the frequency dependence of the imaginary part of $\epsilon(q, \omega - \omega_0)$ by $\omega - \omega_0$ which accounts for the number of excited low-energy particle-hole pairs. Moreover, since the frequency dependence of the absolute value of $\epsilon(q, \omega - \omega_0)$ is weak, we expect the optical conductivity, Eq. (6), to approach

$$\sigma(\omega) = A \left(\frac{\omega_0}{\omega} \right)^3 \left(\frac{\omega}{\omega_0} - 1 \right), \quad (8)$$

where A is a frequency independent amplitude. Indeed, this formula matches the frequency dependence of $\sigma(\omega)$ so closely for the considered adiabatic regime of $\hbar\omega_0/E_f$ that it is indistinguishable from the curve generated by the full weak coupling relation, Eq. 6 (Figs. 8 and 9, continuous lines).

For higher temperatures, $\hbar\omega_0/E_f \ll 1$ is not necessarily true since $\omega_0(T)$ increases considerably (see Table II). Also

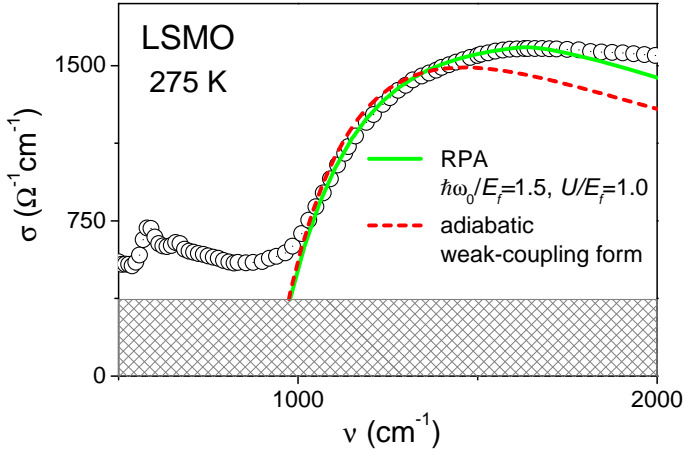


FIG. 10: (Color online) For 275 K: the RPA-approach, Eq. (6), is evaluated with a reduced Fermi energy (a reduction factor of 5 as compared to the 100 K fit which is the continuous line in Fig. 9). The adiabatic weak-coupling form, Eq. (8), still coincides with the full RPA-result and the experimental data along the low frequency slope.

the effective mass of the charge carriers increases with temperature — due to a reduced double exchange — which implies a reduced Fermi energy. For the 275 K data we present in Fig. 10 the evaluation of Eq. (6) with a Fermi energy five times smaller than for the low temperature fit. The dimensionless energy parameters now take the values $\hbar\omega_0/E_f \simeq 1.5$ and $U/E_f \simeq 1$. Obviously, the RPA-result approximates the low frequency slope of the polaronic resonance at 275 K with the same rigor as for 6 K or 100 K. As anticipated, the adiabatic weak-coupling result (Eq. (8), see dashed line in Fig. 10) now does not exactly match the full evaluation but the deviations are still minor. To gain the spectral weight of the measured polaronic resonance, the electron-coupling has to be larger for the 275 K evaluation: $\alpha \simeq 4 - 5$. This is to be expected since, with increasing mass, the coupling should also be enhanced.⁷⁵ Although the weak coupling approach, Eq. (8), is not fully applicable for this intermediate-coupling regime at high temperatures, the result is still so convincing that we propose to discuss all data sets, irrespective of temperature, within the presented approach.

The curves for all considered temperatures have the shape which is approximated by Eq. (8) for low frequencies, with the threshold ω_0 replaced by $\omega_0(T)$. This statement agrees with the conjectured scaling behavior for the low frequency slope, examined at the beginning of the subsection on large polarons — see Fig. 4, in which the low-frequency behavior was actually extrapolated to the “zero line” with Eq. (8). The parameters for this scaling form, the amplitude $A(T)$ and the threshold frequency $\nu_0(T)$, are displayed in Table II.

Shortcomings of the weak coupling approach are the unexplained (temperature dependent) threshold frequency $\omega_0(T)$ and the unmatched slope at the high frequency side when we use a reasonable parameter set in order to reproduce the spectral weight. The coupling parameters are, with this restriction,

in the small coupling regime. The power law decay at the high energy side is ω^{-2} in Eq. (8) whereas the observed power law is closer to ω^{-1} for the 6 K and 100 K data (and approximately $\omega^{-0.3}$ for the 275 K data).

The latter shortcoming should not be taken as a serious flaw of the presented concept. The phase space for excitations increases strongly when the excitation energy deviates from the proximity of the Fermi energy and, moreover, the absorption through such “high energy” excitations is by no means universal. We cannot expect that the simple treatment within RPA with quadratic dispersion can still capture these high-energy excitations correctly.

The failure of the weak coupling approach to account for the (temperature dependent) threshold frequency $\omega_0(T)$ is more disturbing. The threshold in this approach is fixed at the respective frequency of the lattice deformation which will not shift from about 593 cm^{-1} (threshold for 6 K) to 1183 cm^{-1} (threshold for 295 K). Resolving this issue seems to require a type of intermediate-coupling model where the threshold is renormalized but the shape of the absorption spectrum is similar to the shape in the weak coupling approach. A possible scenario is that of Kartheuser, Evrard and Devreese (KED, Ref. 78; see also the review by Mitra *et al.*,⁷⁹ section 2.6, for further references and for a discussion of the literature on this topic). KED propose that the optical absorption for intermediate coupling consists of a relatively narrow zero-phonon peak, assigned to a “relaxed excited state” (RES), and of a broad (multi phonon) sideband, with threshold at ω_{LO} above the zero-phonon peak. Here, ω_{LO} is the frequency of the LO phonon. Consequently the threshold will shift with the frequency of the RES which is dependent on the electron-lattice coupling. This coupling hinges on the electronic band width which in turn depends, for the manganites, on temperature. This scenario implies that a RES resonance exists at ω_{LO} below the polaronic continuum and that it shifts with temperature as the threshold frequency $\omega_0(T)$ in our data. However, such a temperature dependent RES has not been observed as an additional sharp resonance for the manganites, neither in the optical conductivity nor in Raman scattering. For this reason we consider the KED scenario inapt to explain the temperature shift of the threshold in the metallic LSMO films.

In spite of these shortcomings, it should be appreciated that, with respect to the standard polaronic models, this TD-like approach implements a Fermi surface. Short-range Coulomb interactions are included within a controlled weak coupling scheme. Both, Fermi statistics and Coulomb interaction, lead to substantial consequences for the shape of the polaronic absorption spectrum.

As we already pointed out, a dynamical JT effect is miss-

TABLE II: T -dependent parameters of the approximate result for LP, Eq. (8).

T (K)	6	100	160	200	250	275	295
ν_0 (cm^{-1})	593	617	666	765	865	978	1183
A ($10^3 \Omega^{-1} \text{cm}^{-1}$)	18.3	16.3	14.3	12.4	9.5	7.9	6.4

ing in this weak coupling approach. Mannella *et al.* investigated the temperature-dependent JT distortion (see Fig. 3 of Ref. 48). The temperature dependence of the variance of the Mn-O bond length distribution corresponds with the temperature dependent shift of the polaronic MIR excitation for both, LSMO and LCMO (see the inset of Fig. 2 in Ref. 23). It would be highly desirable to have an evaluation which parallels the calculations of Millis, Mueller and Shraiman⁴ for large polarons. For their local modelling they find a temperature dependent shift of the polaronic resonance for sufficiently strong coupling in the undoped case. However, it is not yet conceivable how such a scheme can be set up for extended excitations as the large polarons.

2. Self-trapped polarons

The formation of large polarons in the manganites has been debated before. Röder, Zang and Bishop¹² studied the crossover from a large polaronic state to a quasi-self-trapped state for a single hole in the adiabatic limit, applying a variational technique for the DE model with the inclusion of one effective JT mode. They used a mean-field evaluation for the spin degrees of freedom and neglected other electronic correlation effects. The optical absorption has not been considered in this approach.

Kim, Jung and Noh⁷ propose that their optical conductivity spectra of polycrystalline LCMO ($\text{La}_{0.7}\text{Ca}_{0.3}\text{MnO}_3$) display a sharp Drude peak and a broad MIR absorption band which is to be explained as coherent tunnelling and an incoherent band of large lattice polarons, respectively. They particularly emphasize that, with their electrodynamic analysis, the large polaron should be in a strong coupling regime — a polaronic state which indeed has not been realized in other physical systems because the polaron would usually collapse to a small polaron state for strong coupling. However, it is not obvious how to identify the *large* polarons from their optical conductivity data. A fit to the large polaron picture by Emin²¹, the model to which the authors of Ref. 7 refer to, has not been presented. The steep low-frequency slope of this type of polaronic absorption cannot be resolved in their data. However, since in our thin film optical spectra of LSMO we can clearly identify such a threshold behavior, we will now reinvestigate Emin's phenomenological approach in some detail.

The absorption process arises from exciting a carrier from the ground state in its (self-trapping) potential well to a free-carrier state, invoking the Franck-Condon principle. In this intuitive approach, neither the mechanism which is responsible for the self-trapping nor the nature of the extended states are specified. The optical absorption is calculated by applying Fermi's Golden Rule²¹ which requires the identification of the initial and final charge carrier state. Here we slightly deviate from Emin's evaluation by picking a Gaussian localized state $|G\rangle$ instead of a hydrogenic ground state as initial state. The polaron energy of $|G\rangle$ is lower and it is better confined (see, for example, Ref. 79). The "Gaussian" result for $\sigma(\omega)$ will deviate not significantly from that for the hydrogenic state. The initial localized electronic wave function is $\langle r|G\rangle =$

$(1/R\sqrt{\pi})^{3/2} \exp(-r^2/2R^2)$, and the final free-carrier wave function is $\langle \mathbf{r}|\mathbf{k}\rangle = L^{-3/2} \exp(i\mathbf{k}\mathbf{r})$. Emin assumes free-carrier states with quadratic dispersion $\varepsilon = k^2/2m$ which, for the optical absorption, translates into a frequency dependent wave vector: $k(\omega) = \sqrt{2m(\hbar\omega - E_0)}/\hbar$, where E_0/\hbar is the threshold frequency for the absorption (E_0 is the energy difference between the localized ground state and the lowest continuum state). The optical conductivity is then:

$$\sigma(\omega) = n_p \frac{8\sqrt{\pi}}{3} \frac{e^2}{m} \frac{1}{\omega} (k(\omega)R)^3 e^{-(k(\omega)R)^2} \quad (9)$$

The best fit for the 100 K data is displayed in Fig 8. If we assume that $m = 3m_e$, consistent with specific heat measurements,⁷⁴ and $E_0/h = 543 \text{ cm}^{-1}$ we find a polaron radius from this fit of approximately $R/a \simeq 2.15/\sqrt{3}$, where $a \simeq 3.88 \text{ \AA}$. Correspondingly, the diameter of the polaronic (ground) state is about 2.5 lattice constants (for $m = m_e$, $R/a \simeq 2.15$ the diameter is more than 4 lattice constants). The maximum height of the resonance fixes the prefactor of Eq. (9): the polaron density is estimated for $m = 3m_e$ to a value of $n_p = 3 \times 10^{21} \text{ cm}^{-3}$ (and for $m = m_e$ to $n_p = 10^{21} \text{ cm}^{-3}$). The values for R and n_p are reasonable in this context and support this approach. We point out that the hydrogenic ground state, as introduced by Emin and considered in our previous work, generates a polaron radius which is already unacceptable small.²³

Next we discuss the scaling behavior introduced above (see Fig. 4, upper panel). If we rescale $\sigma(\omega)$ and ω as

$$\hat{\sigma} \equiv \sigma / \left(\frac{8\sqrt{\pi}}{3} \frac{n_p e^2 \hbar}{m E_0} \right) \quad \text{and} \quad w \equiv \frac{\hbar\omega}{E_0}, \quad (10)$$

respectively, and if we also introduce a dimensionless radius

$$\varrho \equiv R\sqrt{2mE_0}/\hbar, \quad (11)$$

we identify the rescaled optical conductivity as

$$\hat{\sigma}(w) = \frac{1}{w} (\varrho \sqrt{w-1})^3 \exp(-\varrho^2(w-1)), \quad (12)$$

which only depends on the dimensionless radius ϱ . If ϱ is independent of temperature, the observed scaling is also true for this approach. For the 100 K data, $\varrho = 1.16 \simeq \sqrt{3/2}$. The fits for the other temperatures produce $\varrho = 1.10 \dots 1.22$ (see Table III), a range which is sufficiently narrow to support the observed scaling within this approach.

Even so, is the experimentally estimated value of $\varrho \simeq \sqrt{3/2}$ supported by theoretical considerations? In the

TABLE III: Self-trapped LP: parameters from Eqs. 9–12 to fit the LSMO MIR spectra at different temperatures for $m = 3m_e$.

T (K)	6	100	160	200	250	275	295
E_0 (cm ⁻¹)	526	543	580	650	777	876	1060
ϱ	1.22	1.17	1.13	1.15	1.14	1.10	1.15
R/a	1.96	1.86	1.73	1.67	1.51	1.37	1.31
n_P (10 ²¹ cm ⁻³)	2.8	2.7	2.6	2.4	2.34	2.26	2.1

Landau-Pekar strong coupling theory with a Gaussian trial wave function (see, for example, Ref. 60) the energy of the localized polaron is $E_p = -(\alpha^2/3\pi)\hbar\omega_{LO}$ and $R = (3\sqrt{\pi/2}/\alpha)\ell$, with the phononic length scale $\ell \equiv \sqrt{\hbar/(2m\omega_{LO})}$. Correspondingly, the polaron binding energy may be reexpressed in terms of the polaron radius: $E_p = -(3/2)(\hbar^2/(2mR^2))$. If we assumed that $|E_p| = E_0$ holds and if we use the above relation between R and ϱ , we would confirm exactly $\varrho = \sqrt{3/2}$. Then, since $\alpha = \sqrt{3\pi}\sqrt{E_0/\hbar\omega_{LO}}$, we would have for the 6 K data $\sqrt{E_0/\hbar\omega_{LO}} \simeq 1 \dots 1.4$ and correspondingly $\alpha = 3 \dots 4$, and for the 295 K data $\sqrt{E_0/\hbar\omega_{LO}} \simeq 1.4 \dots 2$ with $\alpha = 4 \dots 6$. Although this signals the intermediate coupling regime, with non-negligible further corrections to the polaron binding energy, the estimates seem to be in a reasonable range.

However, a serious objection is to be raised against this procedure: E_0 can be identified with $|E_p|$ only if the self-trapped state disappears together with the polarization well in the excitation process. This should not be the case in the considered approach in which we investigate excitations in the adiabatic limit and invoke the Franck-Condon principle. In this limit, we should take $E_0 = 3|E_p|$ (see Emin's review,²¹ or the book by Alexandrov and Mott,⁸⁰ chapter 1.1). With $E_0 = 3|E_p|$ we find $\varrho = 3/\sqrt{2}$ which does not fit the experimental data.⁸¹ Next order corrections to the Landau-Pekar limit do not alleviate this inconsistency.

Assessment of the strong coupling scenario. The resonance in the MIR optical conductivity can be well fitted with Emin's phenomenological strong-coupling approach. Again, the fit is convincing up to frequencies slightly above the maximum whereas the high frequency slope decreases too fast, even faster than for the weak coupling scenario. The observed scaling is approximately reproduced, however with a value for the dimensionless radius ϱ which is inconsistent with a strong coupling estimate.

It is mandatory to ask if this phenomenological approach is trustworthy in terms of microscopic considerations. Alexandrov, Kabanov and Ray⁸² presented numerical results for the Holstein model with two and four sites and up to 50 excited phonons per mode. In fact, the shape of this microscopically calculated polaronic absorption resonance is, for intermediate coupling, similar to that of the phenomenological approach: a steep slope above the threshold and slower decrease at the high frequency side, comparable to the fit curve (Gaussian polaron) in Fig. 8. A direct confirmation of the phenomenological approach was attained for the one-dimensional model.⁸² Hence we consider Emin's approach to be reliable for the considered adiabatic limit.

Despite this positive assessment of the theoretical consistency of the approach we have to question its validity for the metallic manganites. The material (LSMO) is conducting and the effective mass of the charge carriers is supposed to be enhanced but not extremely strong. Consequently, a Fermi surface of the carriers should exist above the mobility edge, at least for low temperatures (we do not explore any details here; for a more comprehensive discussion see the review article by Edwards⁶¹ and the literature cited there, especially

Refs. 83, 84). This implies that if such Gaussian localized polarons exist they have to be excited across the mobility edge to the Fermi surface — not to a band minimum as assumed in the above polaron model.⁸⁵

The consequence now is that the phase space for the excitation of a trapped polaron into “free carrier states” at the hole Fermi surface is large, the density of states is finite, and one expects a step-like increase of the absorption. The experimental shape of the polaronic absorption is, however, not consistent with a (possibly smoothed) absorption-edge step.

Furthermore, one has to account for a mobile charge carrier density of the order of $n = 10^{21} \text{ cm}^{-3}$ to 10^{22} cm^{-3} . This would push the mobility edge⁸⁶ to energies well below the Fermi edge with the consequence that the frequency of the absorption edge is certainly larger than the observed threshold — at least for the low temperature measurements. With this in mind one should dismiss the scenario that all the polarons which contribute to the absorption are self-trapped, that is, localized. They may have a large polaronic mass but they are mostly delocalized. However, Emin's approach decisively depends on localized initial states.⁸⁷ For a transition from a band state to another free-carrier state one again expects a sharp increase of the absorption.⁸⁸ With these impediments it is unlikely that this intuitive approach can be applied directly to the observed polaronic absorption in the LSMO films.

3. Fermi edge singularities

A generalization of the previous considerations (in Sec. IV C 2) to a finite concentration of mobile carrier states is necessary but its implementation is subtle: In the adiabatic limit the localized potential well, formed by the lattice distortion, acts after the excitation of the charge carrier to the Fermi edge as a potential scatterer. Consequently, this limit represents the x-ray edge problem and the power law above the absorption threshold depends on the values of the scattering phase shifts.⁸⁹ It may diverge (the Mahan exciton phenomenon is dominant) or converge (orthogonality catastrophe). Since we have to expect many decay channels for this excitation, the singular diverging edge might well be smoothed so as to reproduce the shape observed in the measurements. The decay at the high energy slope is governed by $\alpha_l = 2\delta_l(k_f)/\pi - \alpha$ where $\delta_l(k_f)$ is the phase shift in the angular momentum channel l and α is the sum over all phase shifts squared (see, for example, Ref. 60). The absorption process involves, according to the standard selection rules, power law behavior with both exponents, $\alpha_{l\pm 1}$. However it is not evident, why $\alpha_{l\pm 1}$ should be so strongly temperature dependent as to reduce the exponent in the power law to the appropriate (T -dependent) value. Nevertheless, α might well increase with more scattering channels available when approaching a disordered paramagnetic state with increasing temperature.

Above, we argued that we do not expect the polarons, which participate in the absorption within the considered frequency window, to be localized. With finite polaron dispersion the situation changes qualitatively^{90,91} because the recoil of the polaronic potential well has to be accounted for. The edge

singularity will form a resonance around the frequency of the direct transitions from the filled valence band to the Fermi edge in the conduction band. This resonance (Mahan exciton) will flatten out when the ratio of the valence band mass to the conduction band mass increases. It is not clear how to identify the polarons with a valence band — or how to quantify a “valence band hole” as the appropriate potential well of the lattice distortion stripped of its charge carrier. In spite of that, the mechanism discussed by Gavoret, Nozières, Roulet and Combescot⁹⁰ and later on by Ruckenstein and Schmitt-Rink⁹¹ is still effective even if the large polarons may not be visualized as forming a valence band of quasi particles. It is the collective behavior associated with the response of the Fermi sea in the course of the excitation process that determines the optical spectrum. However, we have no information on the frequency difference of direct to indirect absorption and we have neither any information if the effective mass of the free carriers at the Fermi surface increases with respect to that of the delocalized polaronic potential well in order to produce the observed temperature dependence of the spectra. To summarize, in a scenario of adiabatic large polarons we have to expect these collective effects of the Fermi sea but it is speculative if they dominate the shape of the optical spectra in the considered frequency window. Furthermore, deviations from the adiabatic limit will contribute to a smoothing of the edge singularity.

V. CONCLUSIONS

We have presented experimental results of the optical conductivity and dc-resistivity in thin films of LSMO and LCMO to analyze polaronic excitations. In both cases the polaron formation energy increases with temperature up to T_{MI} , while the spectral weight diminishes continuously.

Our data indicate different polaronic regimes in both compounds. For LCMO, the SP picture is well accepted, particularly with regard to the high temperature dc-resistivity. The optical conductivity displays an asymmetric Gaussian line shape close to the maximum of the polaronic resonance which also suggests incoherent tunnelling of small polarons. Overall, we conclude that for the Ca-doped compound the SP model with thermally activated transport is approximately valid for both, the ferromagnetic as well as the paramagnetic phase.

In contrast, for LSMO, $\ln(\rho/T)$ deviates from a linear behavior and the optical conductivity has a strong asymmetric line shape with a steep slope at the low frequency side. This shape is typical for LP absorption processes.^{21,22,60} The phenomenological adiabatic LP model by Emin²¹ considers excitations of self-trapped charge carriers to an empty band of free-carrier states, with the polaronic potential-well intact in the adiabatic limit. Emin’s model reproduces the steep low frequency slope with a sufficiently wide maximum but cannot account for the slow decrease on the high frequency side. We challenge that this approach is applicable here because there is no hole-band minimum available to which the excited charge carriers could scatter. The energy difference from the mobility

edge, below which the trapped polarons would reside, to the hole band minimum would have to be the threshold frequency. This frequency E_0/h is (for 6 K) about 526 cm^{-1} , too small for the addressed energy difference. Consequently the modelling has to be modified as to implement LPs with finite mass and a finite density of charge carriers (Fermi edge).

In the weak coupling theory, the generalization of the single polaron absorption by GLF¹⁶ to the situation of many-particle absorption was carried out by Tempere and Devreese.²² The optical conductivity for a similar approach, which is rather based on the Hubbard model than on a Coulomb gas ansatz, is presented in Figs. 8, 9, and 10. The high frequency decay is now better realized through the excitation of particle-hole pairs of the Fermi sea. The scaling of the low-frequency slope (as observed in Fig. 4, upper panel) is implemented through the increase of the number of particle-hole pairs with increasing energy from the Fermi edge. On the other hand, this model cannot account for the shift of the threshold with temperature; the model threshold would always be the LO phonon frequency which is not supposed to shift from 593 cm^{-1} for 6 K to 1183 cm^{-1} for 295 K.

The failure of weak coupling theory necessitates to extend these considerations to intermediate or strong coupling situations, first and foremost in the adiabatic limit. Such an evaluation is still not available and hardly feasible. As we discussed, it involves a collective response of the Fermi sea which leads to singularities in the optical conductivity, well known from the x-ray edge problem. The recoil of the polaronic lattice deformation, which is taken up in the excitation process of the charge carrier to the Fermi edge, will flatten the singularity and might be responsible for the observed shape. Although the proposed consequences for the shape of the absorption spectrum are speculative, the singular response is supposed to be present in any model with a sudden creation of a heavy or localized scatterer in the presence of a Fermi sea.

To summarize, the comparison between the measured optical conductivity spectra and the current theoretical models exhibits their inadequacy to explain the spectral weight at the high frequency slope of the polaronic MIR resonance and the strong shift of the resonance position with temperature. A theoretical solution of the polaron problem which may hold for any electron-phonon coupling, including correlation effects, is highly desirable. The physical quantities that control the temperature dependence for polaron formation, still remain to be elucidated.

Thin films proved to be superior for the analysis of the phononic^{25,26} and polaronic spectra in metallic manganites. We expect that further investigations based on thin film samples will provide considerable additional insight into the physics of the metallic state of the CMR manganites. We refer to an examination of the doping dependence of $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$, the polaronic spectra of which may address the built up of the Fermi surface. We also propose to explore the magnetic field dependence of the thin film spectra in order to address the role of magnetic correlations in the formation of polarons. Finally, $\text{La}_{0.75}(\text{Ca}_{0.45}\text{Sr}_{0.55})_{0.25}\text{MnO}_3$ undergoes an orthorhombic to rhombohedral transition with increasing temperature⁴⁶ which would invite to examine a pos-

sible crossover from SP to LP behavior in the MIR optical conductivity.

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